



JEE (Main)

2021

COMPUTER BASED TEST (CBT)

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Date: 25 July, 2021 (SHIFT-2) | TIME : (3.00 p.m. to 6.00 p.m)

Duration: 3 Hours | Max. Marks: 300

SUBJECT: MATHEMATICS

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**RESULT: JEE (Advanced),
JEE (Main), NEET**

HIGHEST No. of Classroom Selections

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5 AIRs in TOP-50 in JEE (Adv.) 2020 from Classroom

 AIR-2 (GEN-EWS) AIR-15 DHANANJAY	 Zonal Topper IIT-Kharagpur AIR-25 SAMARTH	 2nd Rank in IIT-Kharagpur Zone AIR-29 SANKALP	 AIR-30 AARYAN K.	 AIR-41 UTKARSH P.
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Total Selections in JEE (Advanced) 2020 4505 Classroom: 3441 Distance: 1064	Eligible for JEE (Advanced) Through -JEE (Main) 2020 14755 Classroom: 11047 Distance: 3708	NEET 2020 2646 Classroom: 1833 Distance: 813
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1. If matrix $P = \begin{bmatrix} 1 & 0 \\ 1 & 1 \\ 2 & 1 \end{bmatrix}$, then the matrix P^{50} is equal to

- (1) $\begin{bmatrix} 1 & 0 \\ 50 & 1 \end{bmatrix}$ (2) $\begin{bmatrix} 1 & 0 \\ 25 & 1 \end{bmatrix}$ (3) $\begin{bmatrix} 1 & 0 \\ 75 & 1 \end{bmatrix}$ (4) $\begin{bmatrix} 1 & 1 \\ 25 & 0 \end{bmatrix}$

Ans. (2)

Sol. $P^2 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \\ 2 & 1 & 2 & 1 \end{bmatrix}$

$P^3 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 2 & 1 & 2 & 1 \\ 2 & 1 & 2 & 1 \end{bmatrix}$

$P^4 = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$

Similarly

$P^{50} = \begin{bmatrix} 1 & 0 \\ 25 & 1 \end{bmatrix}$

2. If the first sample A of 100 items has the mean 15 and standard deviation 3 and second sample B has 150 items. If the combined mean and standard deviation of items of both the sample is 15.6 and $\sqrt{13.44}$. Then the standard deviation of items of sample B is :

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Ans. (4)

Sol. Combined mean = 15.6

$$\therefore 15.6 = \frac{100 \times 15 + 150 \times \bar{x}_B}{250}$$

$$\Rightarrow \bar{x}_B = 16 \quad (\text{mean of sample B})$$

Combined standard deviation = $\sqrt{13.44}$

\Rightarrow combined variance (σ^2) = 13.44

$$13.44 = \frac{\sum x_i^2}{250} - 243.36$$

$$\Rightarrow \sum x_i^2 = 64200 \quad \dots\dots\dots(1)$$

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for sample A

$$9 = \frac{\sum x_A^2}{100} - 225$$

$$\Rightarrow \sum x_A^2 = 23400$$

$$\Rightarrow \sum x_{AB}^2 = 64200 - 23400 = 40800$$

standard deviation of sample B will be

$$\sqrt{\frac{40800}{150} - (x_B)^2} = \sqrt{\frac{27200}{150} - 256} = 4 \text{ Ans.}$$

3. The value of $x \in \left[\frac{\pi}{4}, \frac{\pi}{4} \right]$ for which

$$\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$$

(1) $-\frac{\pi}{4}$

(2) $-\frac{\pi}{8}$

(3) $\frac{\pi}{4}$

(4) $\frac{\pi}{8}$

Ans. (3)

Sol. $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$

$R_1 \rightarrow R_1 + R_2 + R_3$

$$\begin{vmatrix} \sin x + 2\cos x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$$

$C_2 \rightarrow C_2 - C_1, C_3 \rightarrow C_3 - C_1$

$$\begin{vmatrix} \sin x + 2\cos x & 1 & 1 \\ \cos x & \sin x - \cos x & 0 \\ \cos x & 0 & \sin x - \cos x \end{vmatrix} = 0$$

$(\sin x + 2\cos x)(\sin x - \cos x)^2 = 0$

$\sin x = \cos x$ or $\sin x = -2\cos x$

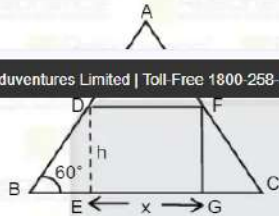
$\tan x = 1$ or $\tan x = -2$

$\therefore x \in \left[-\frac{\pi}{4}, \frac{\pi}{4} \right]$

8. If a rectangle is inscribed in an equilateral triangle of side $2\sqrt{2}$, then the square of maximum area of rectangle is :

Ans. (3)

Sol.



Area of rectangle = $x \cdot h$ (i)

from $\triangle BDE$

$h = BE \tan 60$

$h = \frac{(2\sqrt{2} - x)}{2} \cdot \sqrt{3}$ (ii)

So area, $A = \frac{\sqrt{3}}{2} (2\sqrt{2}x - x^2)$

For maxima $\frac{dA}{dx} = \frac{\sqrt{3}}{2} (2\sqrt{2} - 2x) = 0$

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From (ii) $h = \frac{\sqrt{3}}{2}$

Area = $x \cdot h = \sqrt{3}$

$(\text{Area})^2 = 3$

9. If the coefficients of x^7 and x^8 in the expansion of $\left(2 + \frac{x}{3}\right)^n$ are equal then the value of n is :

(1) 53

(2) 54

(3) 55

(4) 56

Ans. (3)

Sol. $\left(2 + \frac{x}{3}\right)^n = \sum_{r=0}^n {}^nC_r \cdot 2^{n-r} \left(\frac{x}{3}\right)^r$

Coefficient of $x^7 = {}^nC_7 \cdot 2^{n-7} \cdot \left(\frac{1}{3}\right)^7$

Coefficient of $x^8 = {}^nC_8 \cdot 2^{n-8} \cdot \left(\frac{1}{3}\right)^8$

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$\therefore {}^nC_7 \frac{2^{n-7}}{3^7} = {}^nC_8 \frac{2^{n-8}}{3^8}$

$\Rightarrow {}^nC_7 \cdot 6 = {}^nC_8$

$\Rightarrow \frac{6 \cdot n!}{7! \cdot (n-7)!} = \frac{n!}{8! \cdot (n-8)!}$

$\Rightarrow 48 = n - 7 \Rightarrow n = 55$

10. If $f(x) = \begin{cases} \frac{P(x)}{x-2} & ; x \neq 2 \\ \end{cases}$ and $P(x)$ is a polynomial such that $P'(x)$ is constant and $P(3) = 9$. If $f(x)$ is continuous

$1 - 7$; $x = 2$
 at $x = 2$ then find the value of $P(5)$

Ans. (39)

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$$\lim_{x \rightarrow 2} \frac{P(x)}{x-2} = \lim_{x \rightarrow 2} \frac{K(x-2)}{x-2}$$

$$\Rightarrow K(2-\beta) = 7 \dots(1)$$

$$\text{and } P(3) = K(3-2)(3-\beta) = 9$$

$$K(3-\beta) = 9 \dots(2)$$

Divide equation (1) by (2)

$$\frac{2-\beta}{3-\beta} = \frac{7}{9} \Rightarrow \beta = \frac{-3}{2}$$

So, $K = 2$

$$\text{Then } P(x) = 2(x-2) \left(x + \frac{3}{2} \right)$$

$$P(5) = 2 \times (5-2) \times \left(5 + \frac{3}{2} \right) = 39$$

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11. The number of real solutions of the equation $x^2 - |x| - 12 = 0$ is :

- (1) 0 (2) 1 (3) 3 (4) 2

Ans. (4)

Sol. $|x|^2 - |x| - 12 = 0$

$$|x| = 4, -3 \text{ (not possible)}$$

$$\Rightarrow |x| = 4 \Rightarrow x = \pm 4$$

\therefore Number of real solutions = 2

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12. A coin is tossed n times. If the probability of getting at least one head is greater than 0.9, then the minimum value of n is :

- (1) 3 (2) 5 (3) 4 (4) 2

Ans. (3)

$$1 - \left(\frac{1}{2}\right)^n > 0.9$$

$$\Rightarrow 0.1 > \left(\frac{1}{2}\right)^n \Rightarrow n = 4$$

13. Negation of the statement :
 "We will play football only if ground is not wet and there is no sunlight" is:
 (1) We will play football if ground is wet and there is no sunlight.
 (2) We will play football if ground is wet and there is sunlight.
 (3) There is no sunlight and ground is not wet and we will not play football.
 (4) There is sunlight or ground is wet and we will play football.

Ans. (4)

Sol. p : We will play football.
 q : Ground is not wet.
 r : There is no sunlight.

$$\therefore \text{ Given statement is } p \rightarrow (q \wedge r)$$

$$\therefore \text{ Negation is } p \wedge \sim (q \wedge r)$$

$$p \wedge (\sim q \vee \sim r)$$

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14. Let $U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{0, 1, 2, 3, 4, 5\}$, $B = \{4, 5, 6, 7, 8, 9\}$. Then the value of $|A \cap B|$ is _____

(where [.] represents G.I.F.)

- (1) 98 (2) 97 (3) 96 (4) 100

Ans. (4)

Sol. ${}^n C_0 + 3^n C_1 + 5^n C_2 + 7^n C_3 + \dots \dots \dots (n+1) \text{ terms} = \sum_{r=0}^n (2r+1) \cdot {}^n C_r$

$$= 2 \sum_{r=0}^n r {}^n C_r + \sum_{r=0}^n {}^n C_r$$

$$= 2n \cdot 2^{n-1} + 2^n = (n+1) \cdot 2^n$$

15. Evaluate $\int_0^1 \log(x + \sqrt{x^2 + 1}) dx$





Ans. (1)

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Sol. $I = \int_{-1}^1 \log(x + \sqrt{x^2 + 1}) dx$

$$f(x) = \log(\sqrt{x^2 + 1} + x)$$

$$f(-x) = \log(\sqrt{x^2 + 1} - x)$$

$$= -f(x)$$

So $f(x)$ is an odd function.

$$\Rightarrow I = 0$$

16. If ${}^n P_r = {}^n P_{r+1}$ and ${}^n C_r = {}^n C_{r-1}$, then the value of n is :

Sol. ${}^n C_r = {}^n C_{r-1} \Rightarrow \frac{n!}{r!(n-r)!} = 1 \Rightarrow n+1 = 2r \dots \dots (1)$

$$\text{and } {}^n P_r = {}^n P_{r+1} \Rightarrow \frac{n!}{(n-r)!} = \frac{n!}{(n-r-1)!}$$

$$\Rightarrow n-r = 1 \dots \dots (2)$$

$$\text{Solving (1) \& (2) } n+1 = 2(n-1) \Rightarrow n = 3$$

17. Value of $\sum_{n=8}^{100} \left[(-1)^n \frac{n}{2} \right]$ is : (Where [.] represent greatest integer function)

Ans. (4)

Sol. $\sum_{n=8}^{100} \left[(-1)^n \frac{n}{2} \right]$

$$\Rightarrow -1 \times 46 + 50 = 4$$

18. Evaluate $\cot\left(\frac{\pi}{24}\right)$

- (1) $\sqrt{6} - \sqrt{3} + \sqrt{2} - 2$ (2) $\sqrt{6} + \sqrt{3} - \sqrt{2} + 2$ (3) $\sqrt{6} + \sqrt{3} + \sqrt{2} - 2$ (4) $\sqrt{6} + \sqrt{3} + \sqrt{2} + 2$

Ans. (4)

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Sol. $\cot\theta = \frac{\cos\theta}{\sin\theta} = \frac{2\cos^2\theta}{2\sin\theta\cos\theta}$
 $= \frac{1+\cos 2\theta}{\sin 2\theta}$

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$$\frac{\sin \frac{\pi}{12}}{\sin \frac{\pi}{12}}$$
$$\Rightarrow \frac{1 + \frac{\sqrt{3}+1}{2\sqrt{2}}}{\frac{\sqrt{3}-1}{2\sqrt{2}}} = \frac{2\sqrt{2} + \sqrt{3} + 1}{\sqrt{3}-1}$$
$$\Rightarrow \frac{(2\sqrt{2} + \sqrt{3} + 1)(\sqrt{3} + 1)}{2}$$
$$\Rightarrow \frac{2\sqrt{6} + 2\sqrt{2} + 3 + \sqrt{3} + \sqrt{3} + 1}{2} = \sqrt{6} + \sqrt{2} + \sqrt{3} + 2$$

19. If two lines $L_1 = \frac{x-k}{1} = \frac{y-2}{2} = \frac{z-3}{3}$ and $L_2 = \frac{x+1}{3} = \frac{y+2}{2} = \frac{z+3}{1}$ are coplanar. Then the value of k is:

(1) -1 (2) 1 (3) 2 (4) -2

Ans. (2)
 $|k+1 \ 2+2 \ 3+3|$

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$$\Rightarrow (k+1)(-4) - 4(-8) + 6(2-6) = 0$$
$$\Rightarrow (k+1)(-4) = -8$$
$$k = 1.$$

20. If $y = f(x)$ is the solution of differential equation $xdy = (y + x^3 \cos x)dx$ and $f(\pi) = 0$ then $f\left(\frac{\pi}{2}\right)$ is:

(1) $\frac{\pi^2}{4} + \frac{\pi}{6}$ (2) $\frac{\pi^2}{4} + \frac{\pi}{2}$ (3) $\frac{\pi^2}{6} + \frac{\pi}{4}$ (4) $\frac{\pi^2}{6} + \frac{\pi}{6}$

Ans. (2)

Sol. $\frac{xdy - ydx}{x^2} = x \cos x dx$

$$\Rightarrow \int d\left(\frac{y}{x}\right) = \int x \cos x dx$$

$$\Rightarrow \frac{y}{x} = x \sin x + \cos x + c$$

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$$\Rightarrow y = x^2 \sin x + x \cos x + x$$

$$\Rightarrow f\left(\frac{\pi}{2}\right) = \frac{\pi^2}{4} + 0 + \frac{\pi}{2} = \frac{\pi^2}{4} + \frac{\pi}{2}$$

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21. If three vector $\hat{i} + k\hat{j} + b\hat{k}$, $\hat{i} + b\hat{j} + c\hat{k}$ and $a\hat{i} + a\hat{j} + b\hat{k}$ are coplanar then

- (1) $a^2 = bc$ (2) $b^2 = ac$ (3) $c^2 = ab$ (4) $ab = c$

Ans. (2)

Sol. $\begin{vmatrix} 1 & 0 & 1 \\ b & b & c \\ a & a & b \end{vmatrix} = 0$

$$1(b^2 - ac) + 1(ab - ab) = 0 \Rightarrow b^2 = ac$$

22. If \vec{x} & \vec{y} are two vectors such that $|\vec{x}| = |\vec{y}|$ & $|\vec{x} - \vec{y}| = n|\vec{x} + \vec{y}|$, then the angle between \vec{x} & \vec{y}

- (1) π (2) $\pi/2$ (3) $\pi/4$ (4) π/n^2

Ans. (4)

Sol. $|\vec{x} - \vec{y}| = n|\vec{x} + \vec{y}|$

$$x^2 + y^2 - 2xy \cos\theta = n^2(x^2 + y^2 + 2xy \cos\theta)$$

$$x^2(1 + 1 - 2\cos\theta) = n^2 x^2(1 + 1 + 2\cos\theta)$$

$$2(1 - \cos\theta) = 2n^2 \cos\theta$$

$$\cos\theta = \frac{1 - n^2}{n^2 + 1}$$

$$\theta = \cos^{-1}\left(\frac{1 - n^2}{n^2 + 1}\right)$$

23. If combined equation of line $y = p(x)$ and $y = q(x)$ can be written as $(y - p(x))(y - q(x)) = 0$ then angle bisector of $x^2 - 4xy - 5y^2 = 0$ is :

- (1) $x^2 + 3xy + y^2 = 0$ (2) $x^2 + 3xy - y^2 = 0$

Ans. (2)

Sol. Equation of angle bisector of homogeneous equation of pair of straight line $ax^2 + 2hxy + by^2$ is

$$\frac{x^2 - y^2}{a - b} = \frac{xy}{h}$$

for $x^2 - 4xy - 5y^2 = 0$

$a = 1, h = -2, b = -5$

so, equation of angle bisector is

$$\frac{x^2 - y^2}{1 - (-5)} = \frac{xy}{-2}$$

$$x^2 - y^2 + 3xy = 0$$

so, combined equation of angle bisector is $x^2 + 3xy - y^2 = 0$

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24. Equation of a circle is $\text{Re}(z^2) + 2(\text{Im}(z))^2 + 2\text{Re}(z) = 0$ where $z = x + iy$ and a line passes through the vertex of parabola $x^2 - 6x + y + 13 = 0$ and the centre of circle, then y intercept of the line is :

- (1) -2 (2) -1 (3) 2 (4) 1

Ans. (2)

So, $z^2 = x^2 - y^2 + i2xy$

Now $x^2 - y^2 + 2y^2 + 2x = 0$

$$x^2 + y^2 + 2x = 0 \Rightarrow \text{centre} = (-1, 0) \text{ and } x^2 - 6x + y + 13 = 0$$

$$(x-3)^2 = -(y+4)$$

Vertex (3, -4)

$$\therefore \text{Equation of line is } (y-0) = \frac{-4-0}{3+1}(x+1) \Rightarrow 4y = -4(x+1)$$

$$x + y + 1 = 0 \Rightarrow \frac{x}{-1} + \frac{y}{-1} = 1$$

25. If $f(x) = \begin{cases} 5x+1 & ; x < 2 \\ \int_0^x (5+|1-t|)dt & ; x \geq 2 \end{cases}$

(1) $f(x)$ is differentiable $\forall x \in \mathbb{R}$

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(3) $f(x)$ is continuous at $x = 2$ but not differentiable at $x = 1$.

(4) $f(x)$ is neither continuous nor differentiable at $x = 2$.

Ans. (2)

Sol. LHL = $\lim_{x \rightarrow 2^-} (5x+1) = 11$

$$\text{RHL} = \lim_{x \rightarrow 2^+} \int_0^x (5+|1-t|)dt = \int_0^1 (5+(1-t))dt + \int_1^2 (5-(1-t))dt = 11$$

$$f(2) = 11$$

So, $f(x)$ is continuous at $x = 2$

$$\text{LHD at } x = 2 \text{ is } \left. \frac{d}{dx}(5x+1) \right|_{x=2} = 5$$

$$\text{RHD at } x = 2 \text{ is } \left. \frac{d}{dx} \int_0^x (5+|1-t|)dt \right|_{x=2} = 6$$

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